

```

//Outer loop over vertex (test) functions:
for i = 1,2 do {
  //If > -1, m1 is index of a test function  $v_{m_1} \in V_{h,p}$ ,
  //i.e., row in  $S$ :
  m1 := Elem[m].vert_dof[i];
  if (m1 > -1) then {
    //Inner loop over vertex (basis) functions:
    for j = 1,2 do {
      //If > -1, m2 is index of a basis function  $v_{m_2} \in V_{h,p}$ ,
      //i.e., column in  $S$ :
      m2 := Elem[m].vert_dof[j];
      if (m2 > -1) then
        S[m1][m2] := S[m1][m2] + a1*MESI[i][j]/Elem[m].jac
          + a0*Elem[m].jac*MEMI[i][j];
    } //End of inner loop over vertex functions
    //Inner loop over bubble (basis) functions:
    for j = 1,2,...,Elem[m].p-1 do {
      m2 := Elem[m].bubb_dof[j];
      S[m1][m2] := S[m1][m2] + a1*MESI[i][j+2]/Elem[m].jac
        + a0*Elem[m].jac*MEMI[i][j+2];
    } //End of inner loop over bubble functions
    //Contribution of the vertex test function  $v_{m_1}$ 
    //to the right-hand side  $F$ :
    F[m1] := F[m1] +  $\int_{K_a} |J_{K_m}| f^{(m)}(\xi) \varphi_i(\xi) d\xi$ ;
  } //End if (m1 > -1)
} //End of outer loop over vertex functions
//Outer loop over bubble (test) functions:
for i = 1,2,...,Elem[m].p-1 do {
  m1 := Elem[m].bubb_dof[i];
  //Inner loop over vertex (basis) functions:
  for j = 1,2 do {
    m2 := Elem[m].vert_dof[j];
    if (m2 > -1) then
      S[m1][m2] := S[m1][m2] + a1*MESI[i+2][j]/Elem[m].jac
        + a0*Elem[m].jac*MEMI[i+2][j];
  } //End of inner loop over vertex functions
  //Inner loop over bubble (basis) functions:
  for j = 1,2,...,Elem[m].p-1 do {
    m2 := Elem[m].bubb_dof[j];
    S[m1][m2] := S[m1][m2] + a1*MESI[i+2][j+2]/Elem[m].jac
      + a0*Elem[m].jac*MEMI[i+2][j+2];
  } //End of inner loop over bubble functions
  //Contribution of the bubble test function  $v_{m_1}$ 
  //to the right-hand side  $F$ :
  F[m1] := F[m1] +  $\int_{K_a} |J_{K_m}| f^{(m)}(\xi) \varphi_{i+2}(\xi) d\xi$ ;
} //End of outer loop over bubble functions
} //End of element loop

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In Algorithm 2.5 we used the notation $\tilde{f}^{(m)}(\xi) = f(x_{K_m}(\xi))$. If the operator L is space- or time-dependent (for example, if the coefficient functions a_1 and a_0 in the model problem (2.20) are not constant), the precomputed MESI and MEMI arrays cannot be used. Instead, appropriate numerical quadrature must be performed each time the MESI or MEMI arrays in Algorithm 2.5 are accessed.

Efficient implementation of Algorithm 2.5 For the sake of transparency, large portion of Algorithm 2.5 (the application of a given test function to all vertex and bubble basis functions) was repeated two times with minor changes. This part of the code can be moved to a separate subroutine. Moreover, it is not necessary to store the full `Elem[m].bubb_dof`